

DEVELOPMENT  
ECONOMICS

HUMAN CAPITAL



# This Lecture

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- We will talk about **human capital**.
  
- What is human capital?
- How to measure it?
- Can it explain differences in income across countries?
  
- Readings:
  - ▣ Weil's textbook Chapter 6 (sections 6.2 and 6.3)
  - ▣ Paper by Mankiw-Romer-Weil (sections 1, 2, 3.B)

# What is human capital?

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- Even when they have the same tools and environment, some people are more productive than others.
- Some of these qualities share the characteristics of physical capital, so we call them **human capital**.
- Note these qualities are embodied in a **person**.
- Specifically, we can think of human capital in the form of:
  - ▣ **Education.**
  - ▣ **Health.**

# What is human capital?

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- Remember the 5 characteristics of physical capital?
- They all apply to human capital too.
  - It is productive.
    - Healthier and more educated workers produce more.
  - It can be produced.
    - We can spend resources to make people healthier and more educated.
  - Its use is limited.
    - When a worker spends an hour doing something, that is an hour she cannot spend on something else.
  - It can earn a return.
    - People are paid for using their human capital (e.g., more educated people earn more).
  - It wears out.
    - First, people's health deteriorate and we forget the things we learn. Moreover, when a person dies, her human capital disappears.
- Innate talent is not human capital: it may fit 4 of the characteristics above, but it cannot be **produced**.
  - You can invest in getting more education, but you cannot invest in getting more talent.

# Human capital and income differences

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- Can differences in human capital (per capita) explain differences in income (per capita) across countries?
  - ▣ Sounds reasonable. For example, Europeans are on average more educated and healthier than most of the people in developing countries.
- This is what we will study in this lecture.
  - ▣ We will get a similar answer that we got for physical capital: it can explain part of the differences, but not all (or most) of it.
- We will focus mainly on education.
  - ▣ You will study health in the second part of the course

# Education as Human Capital

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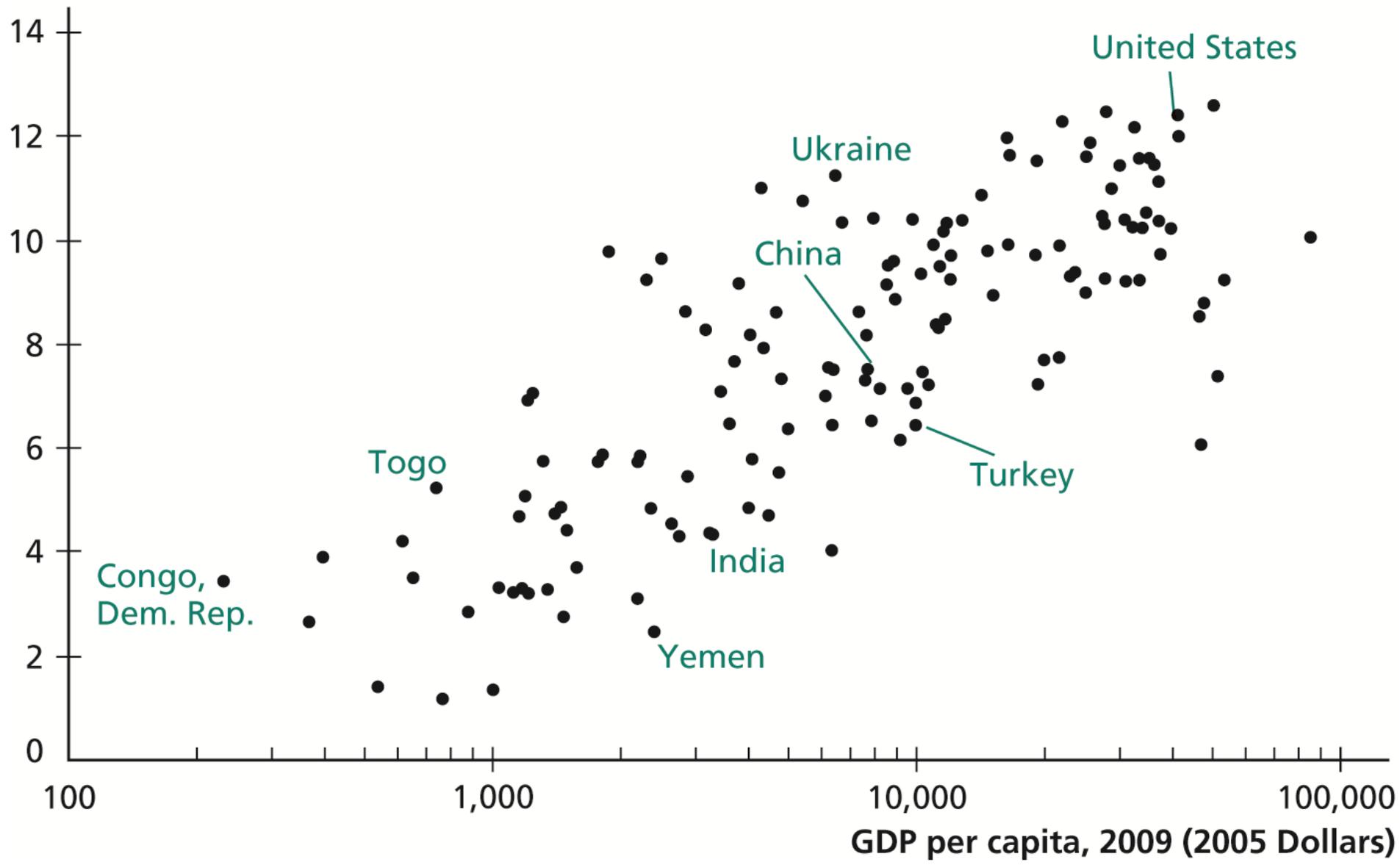
- We all think of education as having value on itself.
  - ▣ “The consumption value” of education
  
- Here, we are more interested in education as human capital, as something that makes people more productive.
  
- We spend resources (physical capital, labor, and human capital) into making more human capital.
  
- Investment in education is very large.
  - ▣ Americans (mostly the government) spend 6.2% of GDP on it.
    - Teacher salaries, buildings, textbooks, financial aid.
  - ▣ This does not count the opportunity cost of student’s time. They are forgoing wages when they are in school.

# Education and Income Differences.

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- Average years of education (in 2000, people age 15+):
  - USA: 12.05
  - Mexico: 6.73
  - India: 4.77
  - Liberia: 2.26
  
- We want to know if these differences in human capital can explain income differences.
  - One (naïve) way to do this: look at the relationship between GDP per capita on years of education.

# Average years of schooling, 2010



# HK and Per Capita GDP: Two Approaches

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- We will add human capital to our “Solow” production function.
  - ▣ Plug real world data on the formula of predicted income per worker.
  - ▣ Compare it to actual income per worker.
    - Just like we did for physical capital (via the saving rate) and population growth.
  - ▣ To do this, we first need to know **human capital’s share of wages**.
  
- We will then look at the MRW paper.
  - ▣ Estimate the “Augmented” Solow model using cross-country regressions
  - ▣ See how the fitted model accounts for the cross-country variation in income
  - ▣ Re-examine the issue of convergence in per-capita income

# Human Capital's Share of GDP

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- From last class: the fraction of GDP paid to owners of capital was about  $1/3$ .
  - ▣ The  $\alpha$  in the production function.
- This means that  $(1 - \alpha) = 2/3$  of GDP is paid to labor.
  - ▣ But, what is the relative fraction that accrues to human capital Vs. the remaining fraction that represents a payment to “raw labor”?

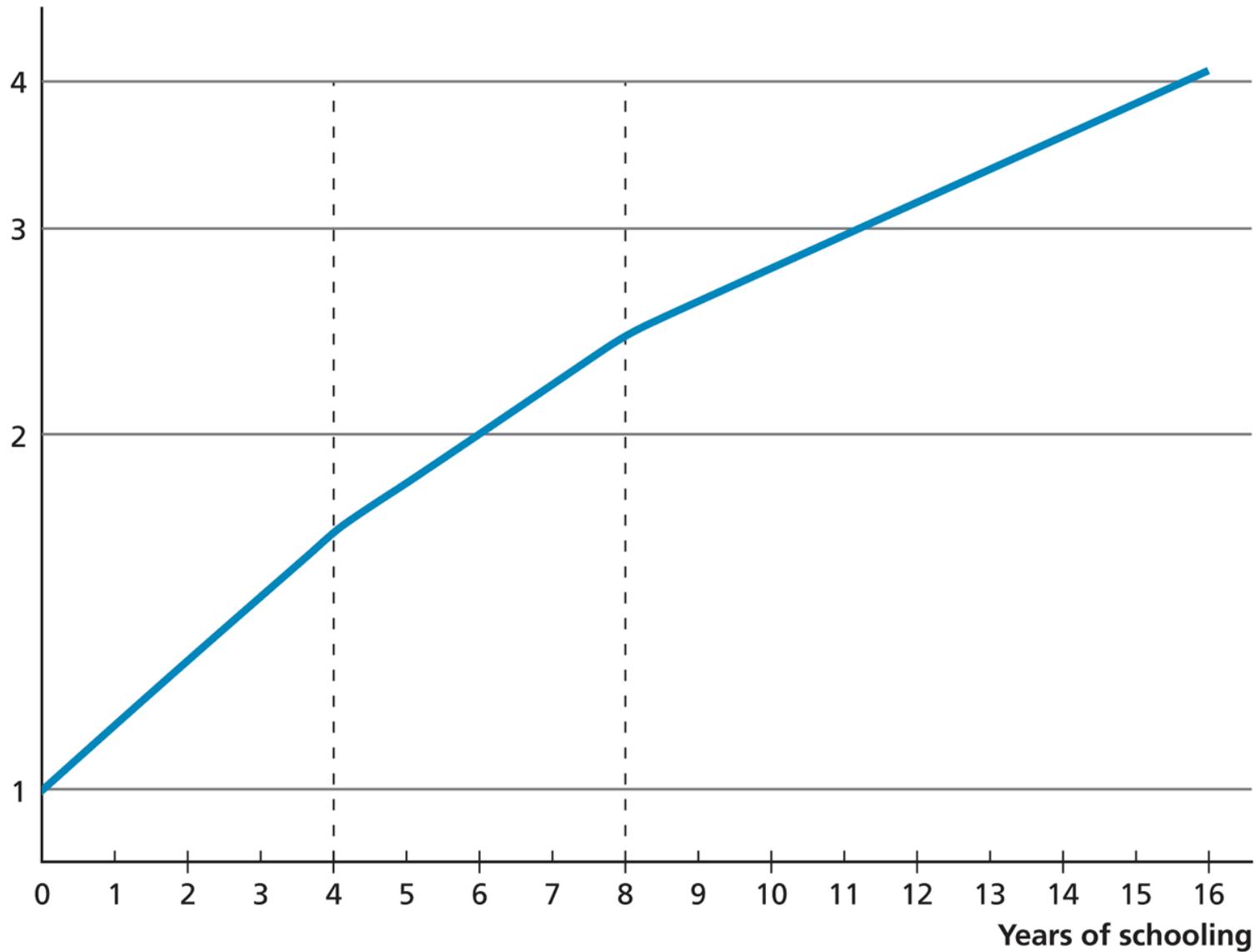
# Education and Wages

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- More educated people earn higher wages.
  - ▣ But by how much?
  
- Hall and Jones (1999) use individual-level (micro) data for multiple countries to get an answer:
  - ▣ An additional year of education is associated with a wage increase of:
    - 13.4% for the first 4 years (grades 1-4).
    - 10.1% for the next four years (grades 5-8).
    - 6.8% for education beyond eight years (high school, college, graduate school).
  
  - ▣ For example, someone with 5 years of schooling earns  $1.134^4 \times 1.101 = 1.82$  times more than someone with zero years of education.

**FIGURE 6.6**  
Effect of Education on Wages

Wage relative to no schooling (ratio scale)



# A digression: Can we trust these estimates of the returns to education?

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- They are achieved by regressing individual log wages on years of education (controlling for experience/age).
  
- Do we get a return of education from this regression?
  - In principle, no.
  - Why? There is the **omitted variable bias** arising from **unobserved “ability”**.
    - Some people are more productive (have more “ability”). This makes them, **by itself**, get higher wages, and also more likely to get more education.
    - The regression coefficient of education also captures the effect of ability.
  - “College graduates would earn more than high school graduates even if they had not gone to college”.

# Addressing the omitted variable bias in the returns to education

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- Several economists tried to address this issue.
  
- The idea is to look at some people that got more schooling due to “**exogenous**” reasons.
  - One source: increases in compulsory schooling.
    - People born in different years are forced to stay longer in school – and this has nothing to do with unobserved ability.
  - Other sources: increases in the supply of schools.
    - College openings through different states and years in the US.
    - Construction of middle schools in developing countries (Indonesia).
  
- In econometrics, these are **instrumental variables** (or just **instruments**).

# Instrumental variable estimates of the returns to education

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- Most instrumental variable estimates are not that different from OLS estimates (like the one from Hall and Jones reported in the textbook).
- For our purposes, the numbers we just saw are in the right ballpark.
- From now on, assume the numbers we saw are the actual returns to education.

# Human Capital's Share of Wages

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- A strong assumption: a person's wage equals her marginal product of labor.
  - ▣ This comes off straight from a firm's profit maximization problem, if firms are "price takers" in the labor market.
  - ▣ We'll relax this assumption in the next class
  
- The wage of a worker with 0 years of education (0 human capital) is called "raw labor".

# Human Capital's Share of Wages

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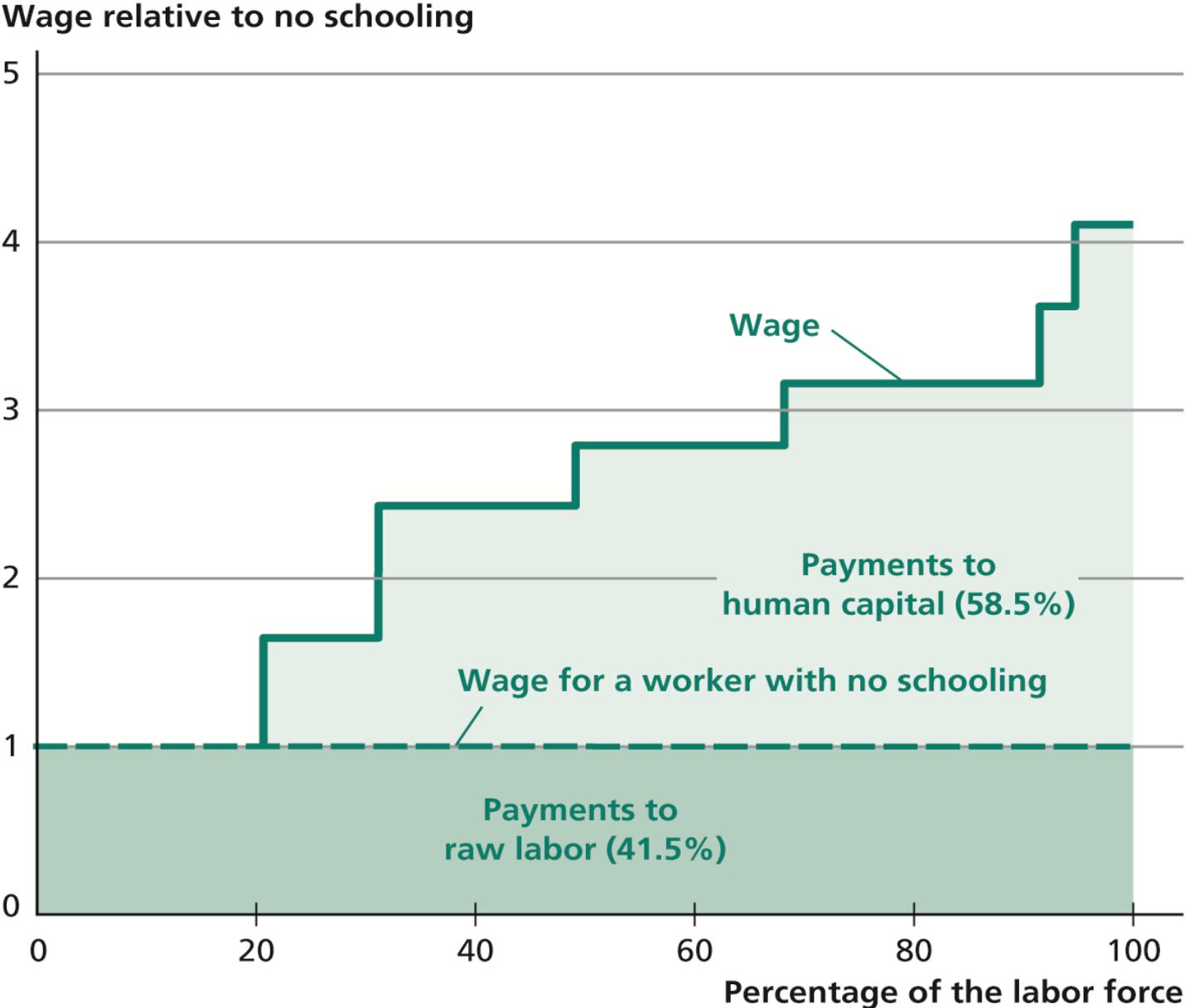
- Difference between the wage of a worker with  $x$  years of education and one with 0 years is the return to  $x$  years of human capital.
  - ▣ Recall: a worker with 5 years of education received a wage 1.82 times higher than one with no schooling.
  - ▣ If the worker with 0 schooling earns \$100, and the one with 5 years earns \$182, we say that \$82 is the part paid to human capital, and \$100 to raw labor.
    - Hence  $0.82/1.82=45\%$  of the human capital share of her wage.
  
- If we do the same for all workers in a country, we can calculate the country-wide share of wages paid to human capital.

**Table 6.2** Breakdown of the Population by Schooling and Wages

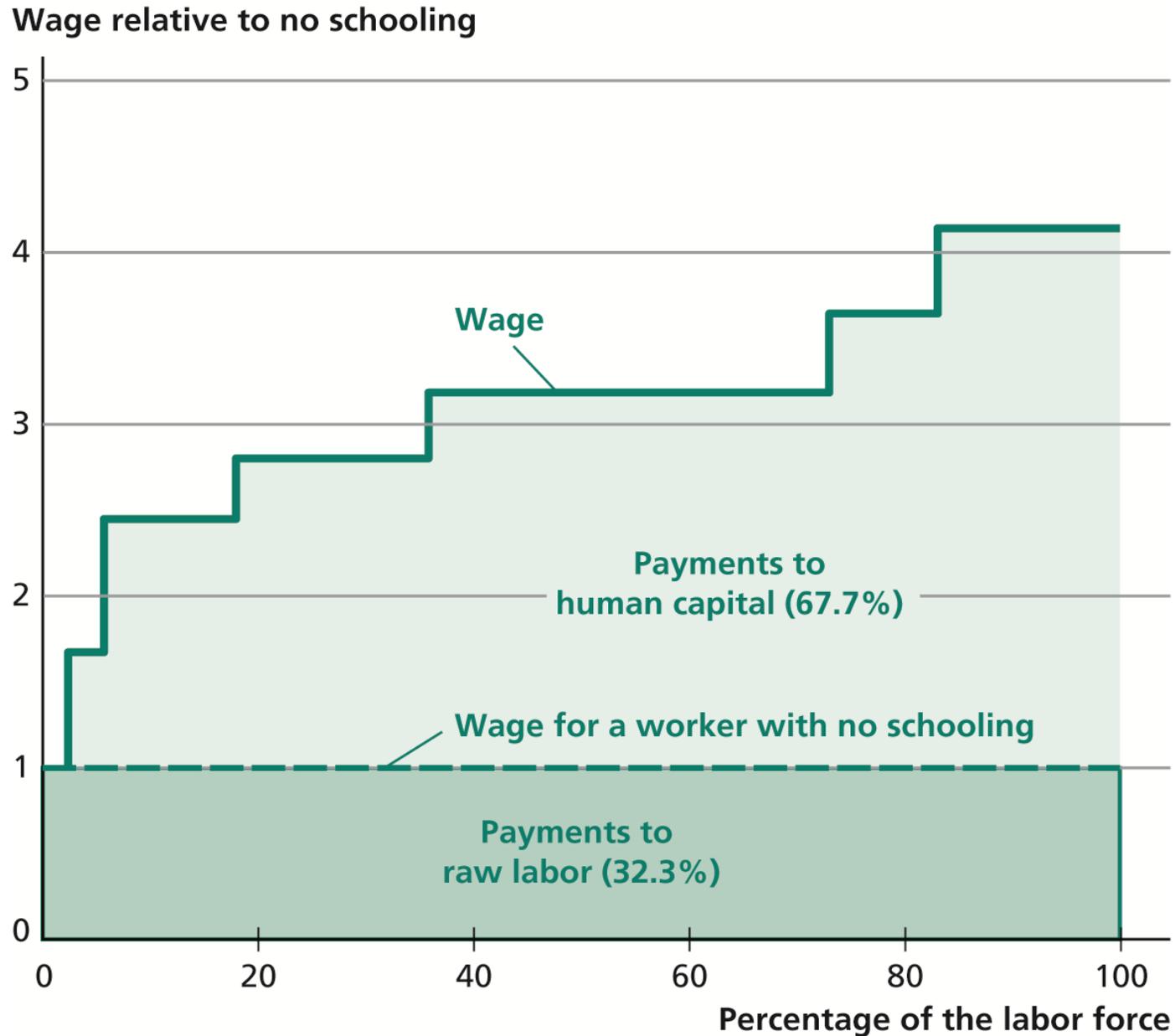
Highest Level of Education	Years of schooling	Wage Relative to No Schooling	Percentage of the Population	
			Developing Countries	Advanced Countries
No Schooling	0	1.00	20.8	2.5
Incomplete Primary	4	1.65	10.4	3.4
Complete Primary	8	2.43	18.0	12.3
Incomplete Secondary	10	2.77	19.3	17.8
Complete Secondary	12	3.16	23.2	37.4
Incomplete Higher	14	3.61	2.9	9.9
Complete Higher	16	4.11	5.3	16.6

*Source:* Barro and Lee (2010).

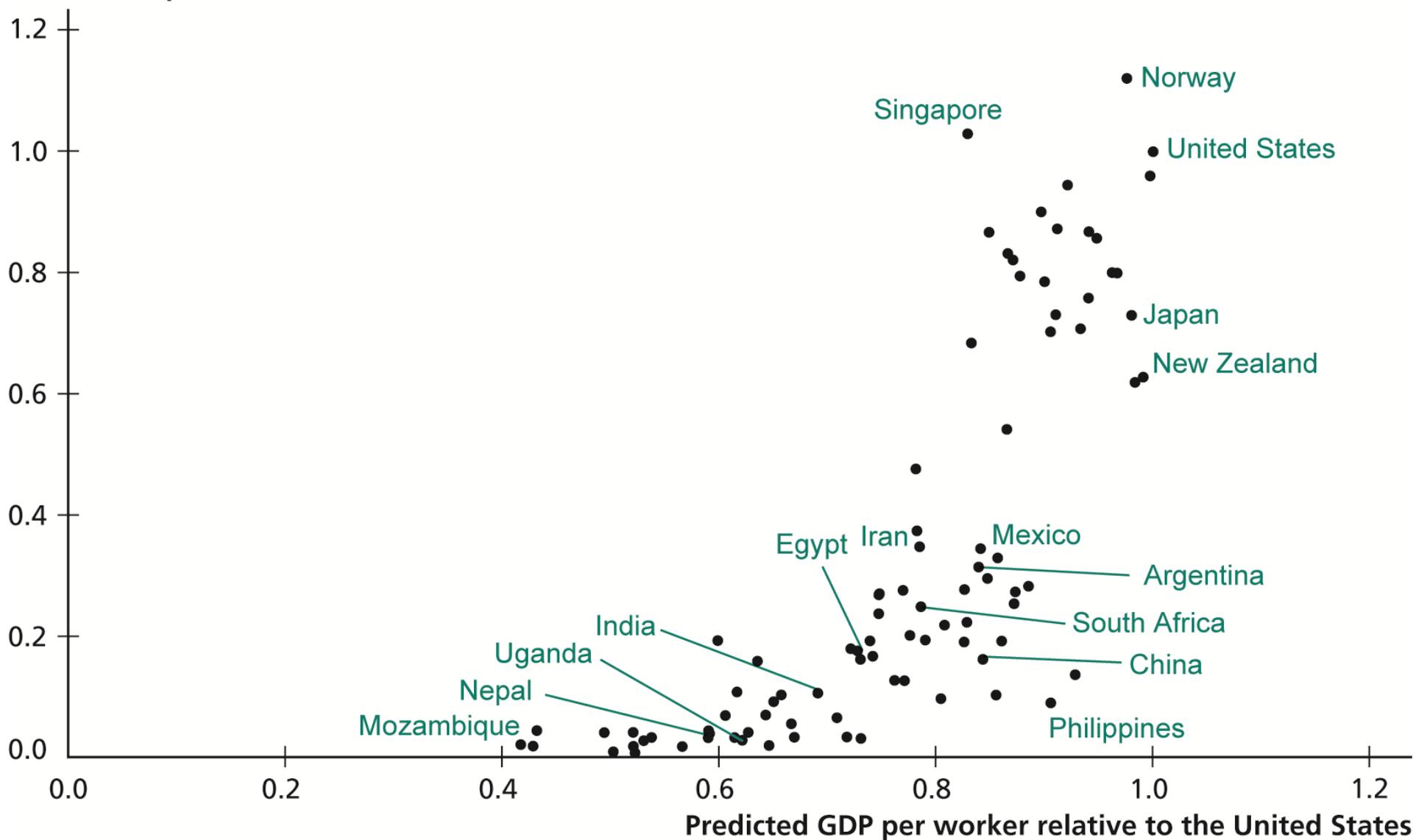
# Share of HK in Wages in Developing Countries



# Share of HK in Wages in Developed Countries



# Actual GDP per worker relative to the United States

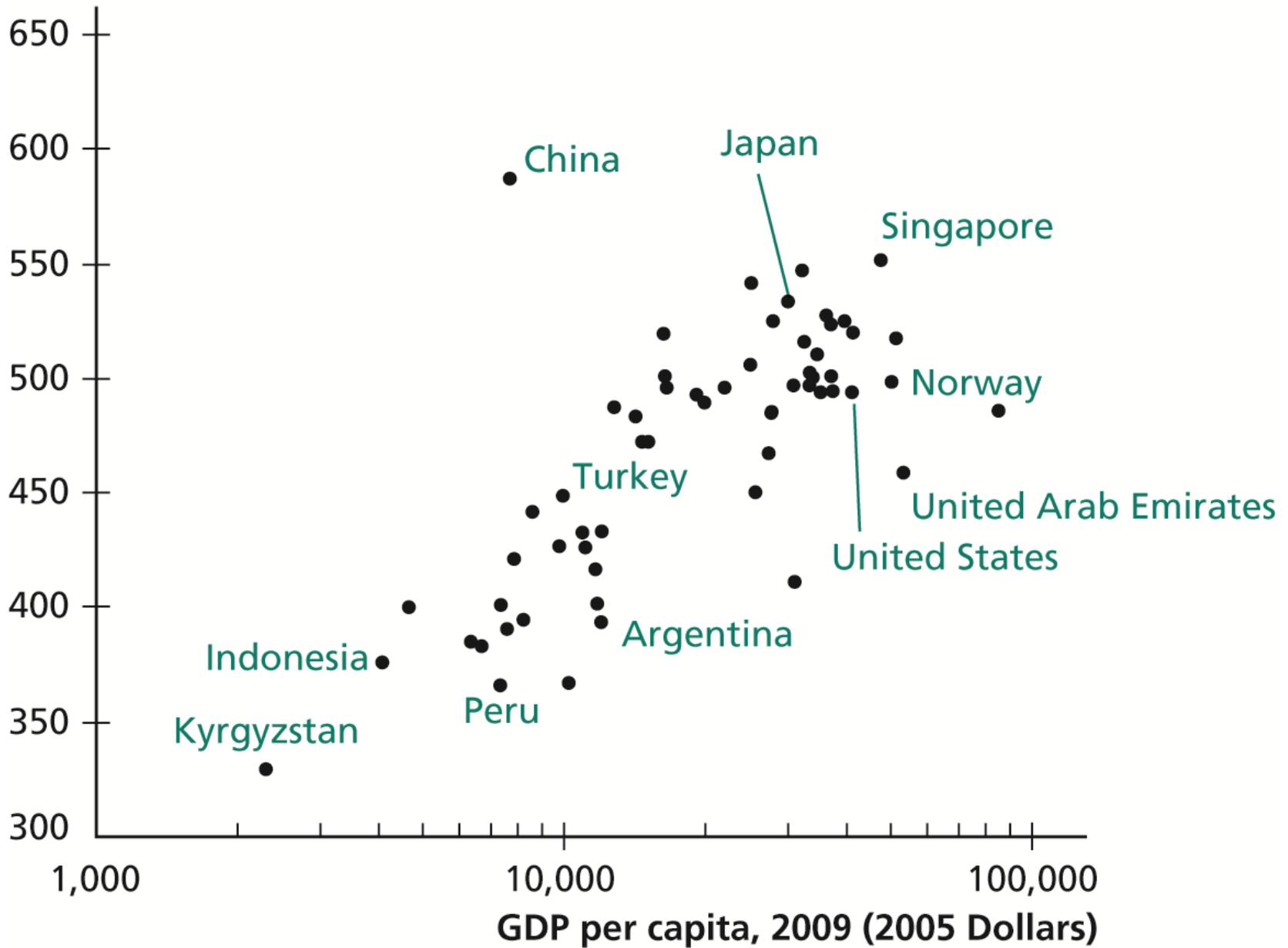


# What are we missing?

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- Quality of education.
  - ▣ One year of schooling in the USA may add more human capital than one year in Uganda.
  - ▣ In the second part of the course, you will study various factors that may explain lower quality of education in low-income countries
  
- Externalities.
  - ▣ We see the **individual** returns to education may be smaller than the **social** returns to education.
    - The educated contribute to society's production in ways they are not remunerated for.
    - This is part of the reason why governments subsidize education

# Average student test scores, 2009



# Mankiw, Romer and Weil (QJE, 1992)

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- This paper rigorously tests the Solow model, in two forms
  - ▣ The “classic” version with physical capital
  - ▣ The “augmented” version with human capital
  
- Main findings are:
  - ▣ Classic Solow model is rejected in the data
  - ▣ Solow model with human capital does a much better job at explaining the cross-country differences in income per capita
  - ▣ Solow model predicts conditional convergence

# The Classic Solow Model

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- Solow model we saw in the last class is:

$$Y(t) = K(t)^\alpha (A(t)L(t))^{1-\alpha} \quad 0 < \alpha < 1.$$

- ▣ Where both L and A are assumed to grow exogenously at rates n and g, respectively.

- Steady state is

$$k^* = [s/(n + g + \delta)]^{1/(1-\alpha)}$$

- ▣ Small k here denotes capital per effective unit of labor: K/AL
- ▣ Here, investment rate is denoted by s

# The Classic Solow Model

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- Substituting this into the production function and taking logs:

$$\ln \left[ \frac{Y(t)}{L(t)} \right] = \ln A(0) + gt + \frac{\alpha}{1-\alpha} \ln(s) - \frac{\alpha}{1-\alpha} \ln(n+g+\delta).$$

- Theoretical predictions:
  - The model implies an elasticity of income per capita with respect to the investment rate of approximately 0.5 ( $\alpha=1/3$  so  $\alpha/(1-\alpha)=0.5$ )
  - And an elasticity of income per capita with respect to changes in all the other factors ( $n+g+\delta$ ) of approximately -0.5.

# From Theory to Empirics

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□ Assumptions:

- $g$  and  $\delta$  are constant across countries:  $g + \delta = 0.05$
- $A(0)$  may vary as it likely reflects initial endowments of technology, resources, climate, institutions, etc.

$$\ln A(0) = a + \epsilon,$$

- $s$  and  $n$  are independent of error term (epsilon above)
- Plugging this into previous equation for income per capita gives:

$$\ln \left( \frac{Y}{L} \right) = a + \frac{\alpha}{1 - \alpha} \ln(s) - \frac{\alpha}{1 - \alpha} \ln(n + g + \delta) + \epsilon.$$

# Estimation Results (I)

Dependent variable: log GDP per working-age person in 1985			
Sample:	Non-oil	Intermediate	OECD
Observations:	98	75	22
CONSTANT	5.48 (1.59)	5.36 (1.55)	7.97 (2.48)
$\ln(I/GDP)$	1.42 (0.14)	1.31 (0.17)	0.50 (0.43)
$\ln(n + g + \delta)$	-1.97 (0.56)	-2.01 (0.53)	-0.76 (0.84)
$\bar{R}^2$	0.59	0.59	0.01
<i>s.e.e.</i>	0.69	0.61	0.38
Restricted regression:			
CONSTANT	6.87 (0.12)	7.10 (0.15)	8.62 (0.53)
$\ln(I/GDP) - \ln(n + g + \delta)$	1.48 (0.12)	1.43 (0.14)	0.56 (0.36)
$\bar{R}^2$	0.59	0.59	0.06
<i>s.e.e.</i>	0.69	0.61	0.37
Test of restriction:			
<i>p</i> -value	0.38	0.26	0.79
Implied $\alpha$	0.60 (0.02)	0.59 (0.02)	0.36 (0.15)

*Note.* Standard errors are in parentheses. The investment and population growth rates are averages for the period 1960–1985.  $(g + \delta)$  is assumed to be 0.05.

# Estimation Results (I)

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- Coefficients on investment rate and population growth have the predicted sign
- Restriction that coeff. on  $\ln(s)$  is equal in magnitude with opposite sign of coeff. on  $\ln(n+g+\delta)$  is not rejected
- Cross-country differences in saving rates and population growth account for a large fraction of the variation in income per capita (adjusted  $R^2=0.59$ )
- Implied  $\alpha=0.6$ , which is much larger than  $1/3$  for the capital share

# Adding Human Capital in the Solow Model

- Let the production function be

$$Y(t) = K(t)^\alpha H(t)^\beta (A(t)L(t))^{1-\alpha-\beta},$$

- Where H is the stock of human capital in the country, which evolves over time as physical capital with investment rate  $s_h$  (and  $s_k$  denotes the investment rate of physical capital)
- Assume that  $\alpha + \beta < 1$  (decreasing return to overall capital)
- Steady state in this model is

$$k^* = \left( \frac{s_k^{1-\beta} s_h^\beta}{n + g + \delta} \right)^{1/(1-\alpha-\beta)}$$

$$h^* = \left( \frac{s_k^\alpha s_h^{1-\alpha}}{n + g + \delta} \right)^{1/(1-\alpha-\beta)}$$

# Adding Human Capital in the Solow Model

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- Substituting steady-state expressions into production function:

$$\ln \left[ \frac{Y(t)}{L(t)} \right] = \ln A(0) + gt - \frac{\alpha + \beta}{1 - \alpha - \beta} \ln(n + g + \delta) \\ + \frac{\alpha}{1 - \alpha - \beta} \ln(s_k) + \frac{\beta}{1 - \alpha - \beta} \ln(s_h).$$

- Theoretical predictions
  - ▣ Coefficient on  $\ln(s_k)$  is now greater than  $\alpha/(1 - \alpha)$
  - ▣ Coefficient on  $\ln(n+g+\delta)$  is larger than coeff on  $\ln(s)$

# From Theory to Empirics

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## □ Assumptions:

- Restrict human capital to education (no health, etc.)
- Proxy the rate of human capital accumulation ( $s_h$ ) in the economy with the percentage of the working-age population that is in secondary school
  - This variable is positively correlated with the investment rate ( $s_k$ ) and negatively correlated with population growth ( $n$ )
- Same assumptions on initial technology, etc as before

$$\ln A(0) = \alpha + \epsilon,$$

# Estimation Results (II)

Dependent variable: log GDP per working-age person in 1985			
Sample:	Non-oil	Intermediate	OECD
Observations:	98	75	22
CONSTANT	6.89 (1.17)	7.81 (1.19)	8.63 (2.19)
$\ln(I/GDP)$	0.69 (0.13)	0.70 (0.15)	0.28 (0.39)
$\ln(n + g + \delta)$	-1.73 (0.41)	-1.50 (0.40)	-1.07 (0.75)
$\ln(SCHOOL)$	0.66 (0.07)	0.73 (0.10)	0.76 (0.29)
$\bar{R}^2$	0.78	0.77	0.24
<i>s.e.e.</i>	0.51	0.45	0.33
Restricted regression:			
CONSTANT	7.86 (0.14)	7.97 (0.15)	8.71 (0.47)
$\ln(I/GDP) - \ln(n + g + \delta)$	0.73 (0.12)	0.71 (0.14)	0.29 (0.33)
$\ln(SCHOOL) - \ln(n + g + \delta)$	0.67 (0.07)	0.74 (0.09)	0.76 (0.28)
$\bar{R}^2$	0.78	0.77	0.28
<i>s.e.e.</i>	0.51	0.45	0.32
Test of restriction:			
<i>p</i> -value	0.41	0.89	0.97
Implied $\alpha$	0.31 (0.04)	0.29 (0.05)	0.14 (0.15)
Implied $\beta$	0.28 (0.03)	0.30 (0.04)	0.37 (0.12)

*Note.* Standard errors are in parentheses. The investment and population growth rates are averages for the period 1960–1985.  $(g + \delta)$  is assumed to be 0.05. SCHOOL is the average percentage of the working-age population in secondary school for the period 1960–1985.

# Estimation Results (II)

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- Ln(School) enters significantly in the income equation
- The presence of schooling reduces the role of investment rate on income per capita
- Investments in (physical+human) capital+population growth jointly explain 80 percent of the cross-country variation in income per capita
- Estimates quantitatively match the theoretical predictions
  - ▣  $\alpha=1/3$ ,  $\beta=1/3$

# Convergence

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- As we discussed in the first class, we can empirically test for convergence in income per capita across countries by regressing the log difference in income per capita between two periods  $t$  and  $t_0$  on  $\log(\text{income}_{t_0})$
- This is called “unconditional convergence”, in the sense that we are not considering that different countries may be converging to different states (as the Solow model predicts!)
- So, a more accurate test of convergence needs to account for the determinants of the steady state: population growth, investment rates in physical and human capital.

# Estimation Results (III)

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Dependent variable: log difference GDP per working-age person 1960–1985

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Sample:	Non-oil	Intermediate	OECD
Observations:	98	75	22
CONSTANT	−0.266 (0.380)	0.587 (0.433)	3.69 (0.68)
ln(Y60)	0.0943 (0.0496)	−0.00423 (0.05484)	−0.341 (0.079)
$\bar{R}^2$	0.03	−0.01	0.46
<i>s.e.e.</i>	0.44	0.41	0.18
Implied $\lambda$	−0.00360 (0.00219)	0.00017 (0.00218)	0.0167 (0.0023)

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*Note.* Standard errors are in parentheses. Y60 is GDP per working-age person in 1960.

# Estimation Results (III)

Dependent variable: log difference GDP per working-age person 1960–1985			
Sample:	Non-oil	Intermediate	OECD
Observations:	98	75	22
CONSTANT	3.04 (0.83)	3.69 (0.91)	2.81 (1.19)
ln(Y60)	-0.289 (0.062)	-0.366 (0.067)	-0.398 (0.070)
ln(I/GDP)	0.524 (0.087)	0.538 (0.102)	0.335 (0.174)
ln( $n + g + \delta$ )	-0.505 (0.288)	-0.551 (0.288)	-0.844 (0.334)
ln(SCHOOL)	0.233 (0.060)	0.271 (0.081)	0.223 (0.144)
$\bar{R}^2$	0.46	0.43	0.65
<i>s.e.e.</i>	0.33	0.30	0.15
Implied $\lambda$	0.0137 (0.0019)	0.0182 (0.0020)	0.0203 (0.0020)

*Note.* Standard errors are in parentheses. Y60 is GDP per working-age person in 1960. The investment and population growth rates are averages for the period 1960–1985. ( $g + \delta$ ) is assumed to be 0.05. SCHOOL is the average percentage of the working-age population in secondary school for the period 1960–1985.

# Estimation Results (III)

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- No unconditional convergence
- After including the determinants of the steady state, the coefficient of  $\log(\text{income}_{t0})$  becomes negative and significant
- Overall, the data seem very much consistent with the predictions of the Solow model once we consider the role of human capital in explaining cross-country income differences